

Astro 350  
Lecture 26  
March 26, 2022

Announcements:

- **Discussion 7 due Wednesday**
- **Homework 7 due Friday**
- Paper abstracts graded—nice job!  
more grades coming soon!

Last time: mapping the Universe  
survey galaxies, map locations in space

*Q: behavior on small scales, at different locations, distances?*

*Q: behavior on large scales, at different locations, distances?*

*Q: lessons?*

# The Large-Scale Structure of the Universe: I

Observations teach us that, to a “first approximation”:  
the Universe *today* is

1. **homogeneous**: average properties same at all points  
e.g., mass density anywhere is same as mass density everywhere!

and

2 **isotropic**: looks same in all directions

universe is homogeneous & isotropic:  
the **“cosmological principle”**  
first guessed(!) by A. Einstein (1917)

~ Q: *as exact (not approximate) statement,  
cosmo principle obviously false! Why?  
In what sense could it be true?*

Example: Cosmo principle and galaxy properties

*Q: if cosmo principle true, how reflected in observations of galaxies at any given time?*

*Q: how could you test this?*

*Q: what does cosmo principle say about how galaxy properties evolve with time?*

Cosmo principle and galaxy properties:

at any given time:

- **average** density of galaxies same everywhere
- distribution of galaxy properties same everywhere  
e.g., types, colors,  $L$ ,  $M$ , ...
- time evolution: must maintain large-scale homogeneity and isotropy

but otherwise, **by itself** principle allows any changes!

# Real Galaxies in the Real Universe

## Beyond the First Approximation

cosmo principle a very good approximation

on large scales ( $\gtrsim 50$  Mpc) www: 2dF

recall  $1 \text{ Mpc} = 10^6 \text{ pc} \sim$  typical distance between galaxies

but do observe **fluctuations** around average galaxy density

www: 2dF maps

on small to medium scales ( $\lesssim 50$  Mpc),

galaxies **clustered** in space:

- loners: “field” galaxy
- few ( $\lesssim 50$ ) galaxies: group
- 100’s-1000’s of galaxies: cluster
- assemblies of groups and clusters: supercluster

# The Logic of the Cosmo Principle

Cosmo Principle:

On large scales ( $\gtrsim 50$  Mpc), universe is

- homogeneous  $\rightarrow$  smooth
- isotropic

*Q: do you need both?*

*Q: e.g., how can you be isotropic but not homogeneous?*

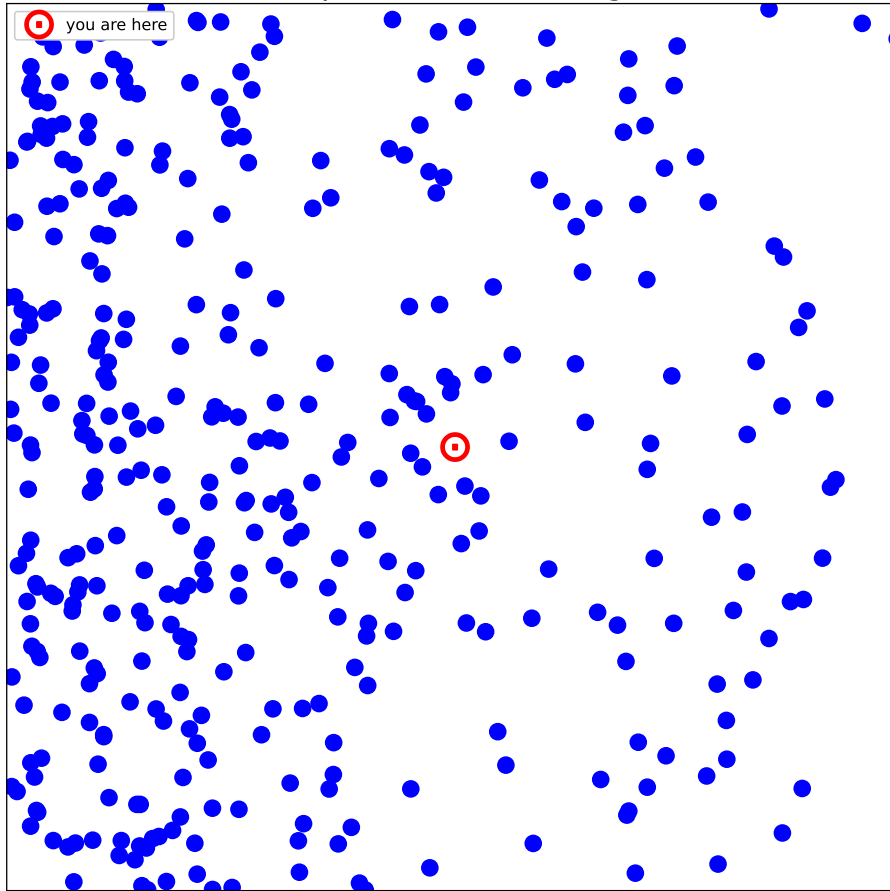
*Q: e.g., how can you be homogeneous but not isotropic?*

Cosmo principle as cosmic democracy:

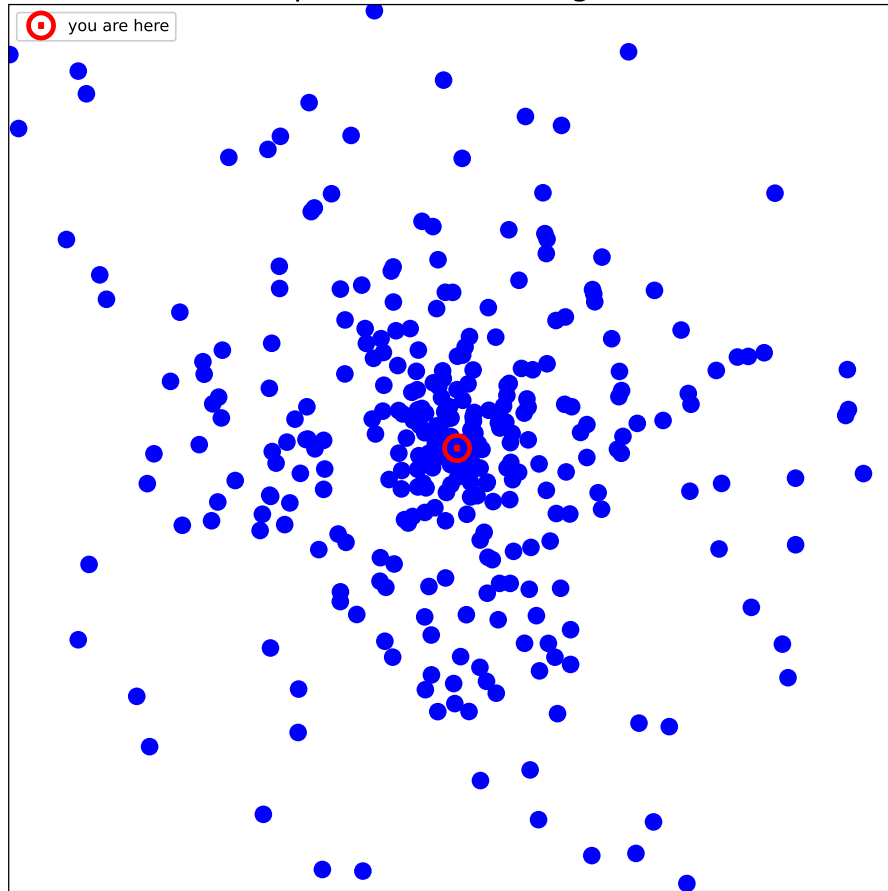
Universe has no center, no edge

- o no special places, directions!

### Not Isotropic and not Homogeneous



### Isotropic but not Homogeneous





## The cosmo principle, in song

I'm just average, common too  
I'm just like him, the same as you  
I'm everybody's brother and son  
I ain't different from anyone  
It ain't no use a-talking to me  
It's just the same as talking to you.

Cosmologist and Nobel Prizewinner Bob Dylan (1964)

## Cosmological Principle: Implications

- demands enormous regularity  
“maximal symmetry” → simplifies analysis!
- places stringent constraints on  
(i.e., simplifies!) the possible nature and behavior  
of the Universe and its contents  
i.e., is “the cosmologist’s friend”
- “trying to tell us something”  
about how universe formed?  
(e.g., cosmic inflation in early universe?)

## iClicker Poll: Cosmodynamics

galaxies have mass → gravitate  
in general, expect galaxies to be in motion

What pattern of motions (relative to us) will we find?

- A most galaxies move towards us
- B roughly half move away, half towards us
- C most galaxies move away from us

## iClicker Poll: Cosmodynamics Twofer

in fact: the *majority* of galaxies move away from us

What percentage of galaxies are observed to move away?

- A between 50% and 75%
- B between 75% and 90%
- C between 90% and 95%
- D between 95% and 99%
- E > 99%

# Cosmodynamics I

of  $> 1$  million galaxies with redshift/blueshift measurements

$< 20$  galaxies have blueshifts! (only nearest ones)

so:  $> 99.9999\%$  of galaxies have redshifts!

$\Rightarrow$  essentially all galaxies have **redshift**:

$$z \equiv \frac{\lambda_{\text{obs}} - \lambda_{\text{rest}}}{\lambda_{\text{rest}}} > 0 \quad (1)$$

$\rightarrow$  move away!

line-of-sight speed: Doppler law sez  $v = cz$

first approximation:

Hubble (1929)  $v$  & distance  $r$  related:

$\bar{\omega}$  www: Hubble original data

*Q: how are  $v$  and  $r$  related mathematically?*

Hubble: galaxy speed and distance *proportional*

$$\Rightarrow v \propto r$$

$$v = H_0 r \quad \text{Hubble law}$$

in fact:  $\vec{v} = H_0 \vec{r}$

that is, speed and distance **directions** the same

→ galaxies all move *radially* away from us!

*Q: why did it have to be this way?*

## Hubble Law $v = H_0 r$

Hubble parameter (a.k.a. “Hubble constant”)

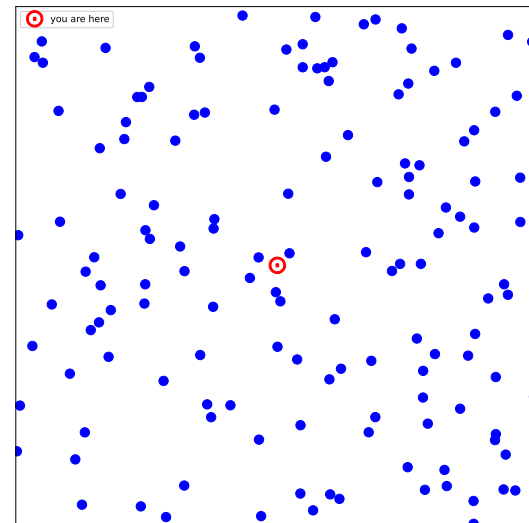
$$H_0 \simeq 72 \text{ km s}^{-1} \text{ Mpc}^{-1} \quad (2)$$

e.g., galaxy at  $r = 10 \text{ Mpc}$  moves away at  $720 \text{ km/s}$

Try it!

draw  $\vec{v}$  on galaxies

*Comment on pattern*



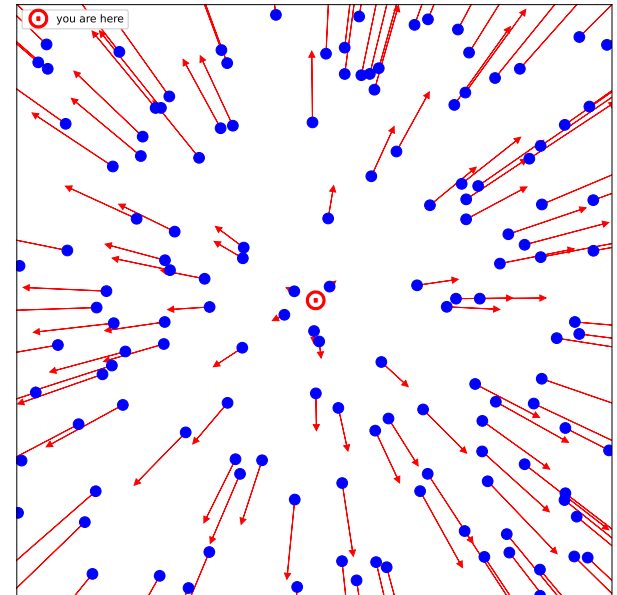
# Structure + Dynamics: Evolution

observe:

- U. homogeneous, isotropic
- Hubble law  $v = Hr$

i.e., galaxies smoothly spread in space  
yet moving too

and motions all directed away from us!  
so velocity pattern “points back to us”



*Q: how reconcile?*

at least 2 logical possibilities...



# 1. “Egoist” interpretation: we are at the center of U.

Imagine galaxies all launched from same point (here)

initially: each launched with different speed  $v_{\text{gal}}$

afterwards: each coasts, keeping its  $v_{\text{gal}} = \text{const}$

Then after time  $t$ , a galaxy seen at distance  $r = v_{\text{gal}}t$

so  $r \propto v_{\text{gal}} \Rightarrow$  farther = faster: Hubble!

In this picture: Hubble law means  $r = v_{\text{gal}}t = H_0 r t$

so “coasting time “ is  $t_H = 1/H_0 = 14 \times 10^9 \text{ yr} = 14 \text{ billion yrs}$

**“Hubble time”**\* – “egoist” age of Universe

and since max “launch” speed is  $v_{\text{gal}} < c$

expect “edge” of galaxy sphere

at radius  $d_H = ct_H = c/H_0 = 4200 \text{ Mpc}$

**“Hubble Radius/Length”**\* – “egoist” size of Universe

\*When egoism is discarded, we’ll reinterpret the Hubble length & time, but still find both useful & interesting numbers

So “egoist” picture gives Hubble’s law!

Logically possible! But...

*Q: give a philosophical reason why we don’t believe this*

*Q: give a physical reason why this treatment can’t be right?*

*Q: give an observational reason why we don’t believe this*

# Critiques of Cosmic Egoism

We are at the center of the universe?

Philosophically:

- not Copernican (violates “principle of mediocrity” )

Physically:

- haven't included gravity!

Observationally:

- Milky Way, local galaxies don't look special  
not what expect from center of explosion  
compare supernova → distinctive neutron star/BH at center
- no evidence for “edge” to Universe at great distances

## 2. Einstein interpretation of Hubble's law:

using General Relativity:

**Universe is expanding**

that is, **space itself is expanding!**

recall: this is possible, since GR says spacetime is dynamic!

But this implies that

- all galaxies receding from all others
- and they do so because they are “riding” on points within an expanding grid!

imagine rubber graph paper being stretched!

bold, strange idea!

*demo: expanding universe*

*Q: implications?*

## The Magic of Hubble

*Somewhat technical derivation:*

consider three arbitrary cosmic points:

$$\vec{r}_{BC} = \vec{r}_{AC} - \vec{r}_{AB}$$

Assume  $A$  sees Hubble's law:

- $\vec{v}_{AB} = H\vec{r}_{AB}$
- $\vec{v}_{AC} = H\vec{r}_{AC}$

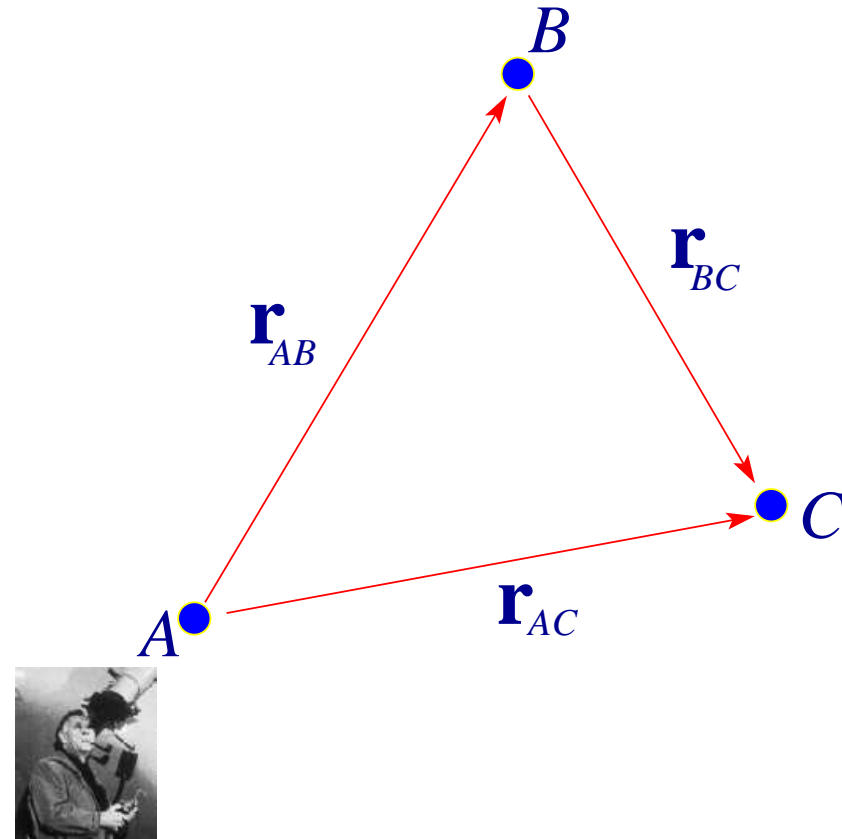
Then ask: *what does  $B$  see?  $C$ ?*

find velocities relative to  $B$ :

$$\vec{v}_{BC} = \vec{v}_{AC} - \vec{v}_{AB} = H(\vec{r}_{AC} - \vec{r}_{AB}) = H\vec{r}_{BC}$$

This is huge!

Q: *why? What have we proven?*



we have shown:

if  $A$  sees Hubble's law, then so do (arbitrary)  $B$  and  $C$

thus: if *any* observer measures Hubble's law

then *all* observers will measure Hubble's law!

so: Hubble law implies

→ *all* galaxies recede according to same law

→ *no need for center, space has no special points*

Moreover: Hubble law is *only* motion

which preserves homogeneity and isotropy

i.e., *any* other motion breaks cosmo principle

...but Hubble law is exactly what's observed!

## Revolution Re-Re-Re-Visited

### **Copernican Revolution I (17th Century):**

Earth is one typical planet among many  
not center of solar system

### **Copernican Revolution II (earth 20th Century):**

Sun is one typical star among many  
not center of Milky Way Galaxy

### **Copernican Revolution III (1920's):**

Milky Way is one typical galaxy among many  
Universe much larger than previously thought

### **Copernican Revolution III (late 20th century):**

most matter in the U is weakly interacting dark matter  
we are not even made of the dominant stuff

### **Copernican Revolution IV (20th century):**

Universe is homogeneous on large scales,  
and has no center

... stay tuned for more...